

5.31/3

$$a) \int_{-2}^{1,2} (3x^2 - x + 2) dx = \left[ x^3 - \frac{1}{2}x^2 + 2x \right]_{-2}^{1,2}$$

$$= 1,2^3 - \frac{1}{2} \cdot 1,2^2 + 2 \cdot 1,2 - \left( (-2)^3 - \frac{1}{2} \cdot (-2)^2 + 2 \cdot (-2) \right) = 3,408 - (-14) = \underline{\underline{17,408}}$$

$$b) \int_1^5 3 \left( \frac{5}{z} + 2z \right) dz = 3 \cdot \int_1^5 \left( 5 \cdot \frac{1}{z} + 2z \right) dz = 3 \cdot \left[ 5 \ln|z| + z^2 \right]_1^5$$

$$= 3 \cdot \left( 5 \ln 5 + 5^2 - \left( \underset{=0}{5 \ln 1 + 1^2} \right) \right) = 3 \cdot (5 \ln 5 + 24) \approx \underline{\underline{96,14}}$$

$$c) \int_{-4}^4 \frac{1}{2} x (2+t)^2 dx = \frac{1}{2} (2+t)^2 \cdot \int_{-4}^4 x dx = \frac{1}{2} (2+t)^2 \cdot \left[ \frac{1}{2} x^2 \right]_{-4}^4$$

$$= \frac{1}{2} (2+t)^2 \cdot \left( \frac{1}{2} \cdot 4^2 - \frac{1}{2} \cdot (-4)^2 \right) = \underline{\underline{0}}$$

$$d) \int_2^4 \sqrt{2x+4} dx = \int_2^4 (2x+4)^{\frac{1}{2}} dx = \left[ \frac{1}{2} \cdot \frac{2}{3} (2x+4)^{\frac{3}{2}} \right]_2^4$$

$$= \frac{1}{3} \cdot 12^{\frac{3}{2}} - \frac{1}{3} \cdot 8^{\frac{3}{2}} \approx \underline{\underline{6,31}}$$

$$e) \int_{4,5}^3 \left( \frac{2}{t^2} + \frac{2}{t} \right) dt = 2 \cdot \int_{4,5}^3 \left( t^{-2} + \frac{1}{t} \right) dt = 2 \cdot \left[ -t^{-1} + \ln|t| \right]_{4,5}^3$$

$$= 2 \cdot \left( -\frac{1}{3} + \ln 3 - \left( -\frac{1}{4,5} + \ln 4,5 \right) \right) = 2 \cdot \left( -\frac{1}{3} + \ln 3 - \ln 4,5 \right) \approx \underline{\underline{-1,033}}$$

$$f) \int_{-3}^{-1} (-x^3 + 2e^x) dx = \left[ -\frac{1}{4}x^4 + 2e^x \right]_{-3}^{-1} = -\frac{1}{4} + \frac{2}{e} - \left( -\frac{81}{4} + \frac{2}{e^3} \right) \approx \underline{\underline{20,64}}$$

$$g) \int_4^1 \frac{2+2z}{z^2+2z+1} dz = \int_4^1 \frac{2(1+z)}{(z+1)^2} dz = \int_4^1 \frac{2}{z+1} dz = 2 \cdot \left[ \ln|z+1| \right]_4^1$$

$$= 2 (\ln 2 - \ln 5) \approx \underline{\underline{-1,83}}$$

$$h) \int_{-1}^{0,5} 6e^{4x-1} \cdot e^{2x} dx = \int_{-1}^{0,5} 6 \cdot e^{6x-1} dx = \left[ e^{6x-1} \right]_{-1}^{0,5} = e^2 - e^{-7} \approx \underline{\underline{7,388}}$$

$$i) \int_1^3 (4u - 2 \ln u) du = 2 \cdot \int_1^3 (2u - \ln u) du = 2 \cdot \left[ u^2 - (u \ln u - u) \right]_1^3$$

$$= 2 \cdot \left[ u^2 - u \ln u + u \right]_1^3 = 2 (9 - 3 \ln 3 + 3 - (1 - 1 \ln 1 + 1)) =$$

$$= 2 \cdot (10 - 3 \ln 3) = 20 - 6 \ln 3 \approx \underline{\underline{13,408}}$$

$$k) \int_1^{\pi} \left( \frac{1}{x} + 2 \sin x \right) dx = \left[ \ln|x| - 2 \cos x \right]_1^{\pi} = \ln \pi - 2 \cos \pi - \left( \ln 1 - 2 \cos 1 \right)$$

$$= \ln \pi + 2 + 2 \cos 1 \approx \underline{\underline{4,225}} \quad (\text{TR auf RAD!})$$

$$l) \int_1^4 \frac{5t}{t^2+1} dt - \int_1^4 \frac{3t}{t^2+1} dt = \int_1^4 \frac{2t}{t^2+1} dt = \left[ \ln|t^2+1| \right]_1^4 = \ln 17 - \ln 2 \approx \underline{\underline{2,140}}$$

$$m) \int_0^{-2} \frac{2}{(1-x)^2} dx = 2 \cdot \int_0^{-2} (1-x)^{-2} dx = 2 \cdot \left[ -1 \cdot (-1) \cdot (1-x)^{-1} \right]_0^{-2} = 2 \left( \frac{1}{3} - 1 \right) = \underline{\underline{-1\frac{1}{3}}}$$



5.32/6

$$a) \int e^{2-2t} dt = -\frac{1}{2} \cdot e^{2-2t} + C; \quad c \in \mathbb{R}$$

$$b) \int 4 \cos(4x) dx = \sin(4x) + C; \quad c \in \mathbb{R}$$

$$d) \int_{-a}^a x^2 dx = 10$$

$$\left[ \frac{1}{3} x^3 \right]_{-a}^a = \frac{1}{3} a^3 - \frac{1}{3} (-a)^3 = \frac{2}{3} a^3 \stackrel{!}{=} 10 \quad | \cdot \frac{3}{2}$$

$$a^3 = 15$$

$$a = \sqrt[3]{15} \approx 2,466$$

$$d) \int \frac{(t-1)(t+1)}{2t^3-2t} dt = \int \frac{(t-1)(t+1)}{2t(t-1)(t+1)} dt = \int \frac{1}{2t} dt = \frac{1}{2} \ln|t| + C; \quad c \in \mathbb{R}$$

$$e) \int 6 \sin(3t+3) dt = 2 \cdot \int 3 \sin(3t+3) dt = 2 \cdot (-\cos(3t+3)) + C \\ = -2 \cos(3t+3) + C; \quad c \in \mathbb{R}$$

$$f) \int_1^a \left( \frac{1}{4} x^3 - 8x \right) dx = -4$$

$$\left[ \frac{1}{16} x^4 - 4x^2 \right]_1^a = \frac{1}{16} a^4 - 4a^2 - \left( \frac{1}{16} - 4 \right) = \frac{1}{16} a^4 - 4a^2 + \frac{63}{16}$$

$$\frac{1}{16} a^4 - 4a^2 + \frac{63}{16} = -4 \quad | +4$$

$$\frac{1}{16} a^4 - 4a^2 + \frac{127}{16} = 0 \quad | \cdot 16$$

$$a^4 - 64a^2 + 127 = 0$$

Substitution:  $z := a^2$

$$z_{1/2} = \frac{64 \pm \sqrt{64^2 - 4 \cdot 1 \cdot 127}}{2} = 32 \pm \sqrt{897}$$

$$a_{1/2} = \pm 7,87; \quad a_{3/4} = \pm 1,432$$

$$g) \int_{-2}^a \left( -\frac{2}{u^2} + 2u \right) du = -3$$

$$\left[ \frac{2}{u} + u^2 \right]_{-2}^a = \frac{2}{a} + a^2 - \left( \frac{2}{-2} + 4 \right) = \frac{2}{a} + a^2 - 3 \stackrel{!}{=} -3$$

$$\frac{2}{a} + a^2 = 0 \quad | \cdot a$$

$$2 + a^3 = 0$$

$$\Rightarrow a = \sqrt[3]{-2} \approx -1,26$$

532/6

$$a) \int_{-\pi}^a 3 \sin x \, dx = 0$$

$$\cos(-\pi) = \cos \pi$$

$$[-3 \cos x]_{-\pi}^a = -$$

$$= -3 \cos a - (-3 \cos(-\pi))$$

$$= -3 \cos a - (-3 \cos \pi)$$

$$= -3 \cos a + 3 \cos \pi = \underset{\neq 0}{-3} (\cos a - \cos \pi) \stackrel{!}{=} 0$$

$$\cos a = \cos \pi$$

$$\Rightarrow a = \pi \text{ bzw. } a = (2k+1)\pi$$

k ∈ Z

